



Why did we elaborate an entangled photons experiment in our engineering school?

Ecole Supérieure d'Optique

Lionel Jacubowicz

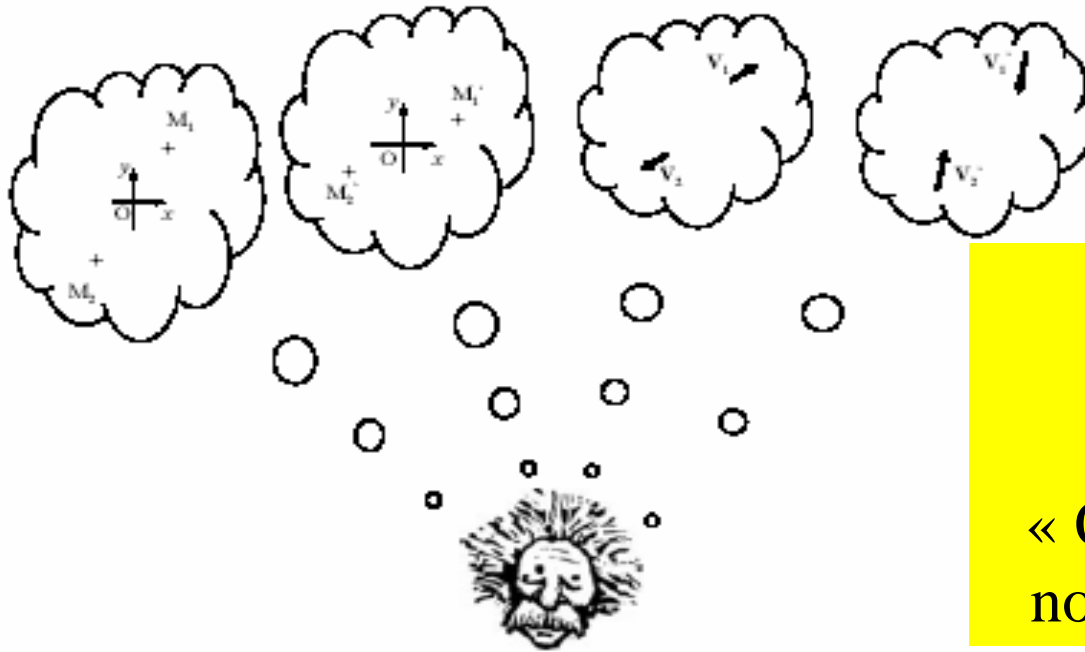
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Tél : 33(0)1 69 35 87 18***

1935 : Quantum Mechanics allows strange entangled states



EPR Paradox

« Quantum Mechanics is not a *complete* theory »

Gedankenexperiment on entangled states

Einstein, Podolsky, et Rosen (1935)



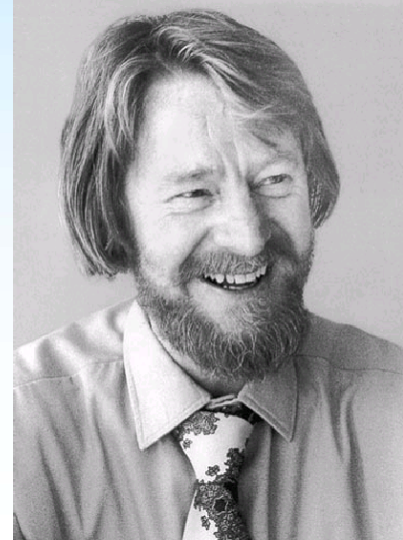
1935 : Quantum Mechanic allows strange entangled states

1964 : Bell Theorem

« It is impossible to reproduce all Quantum Mechanics predictions with any Hidden Variable Local Theory. »

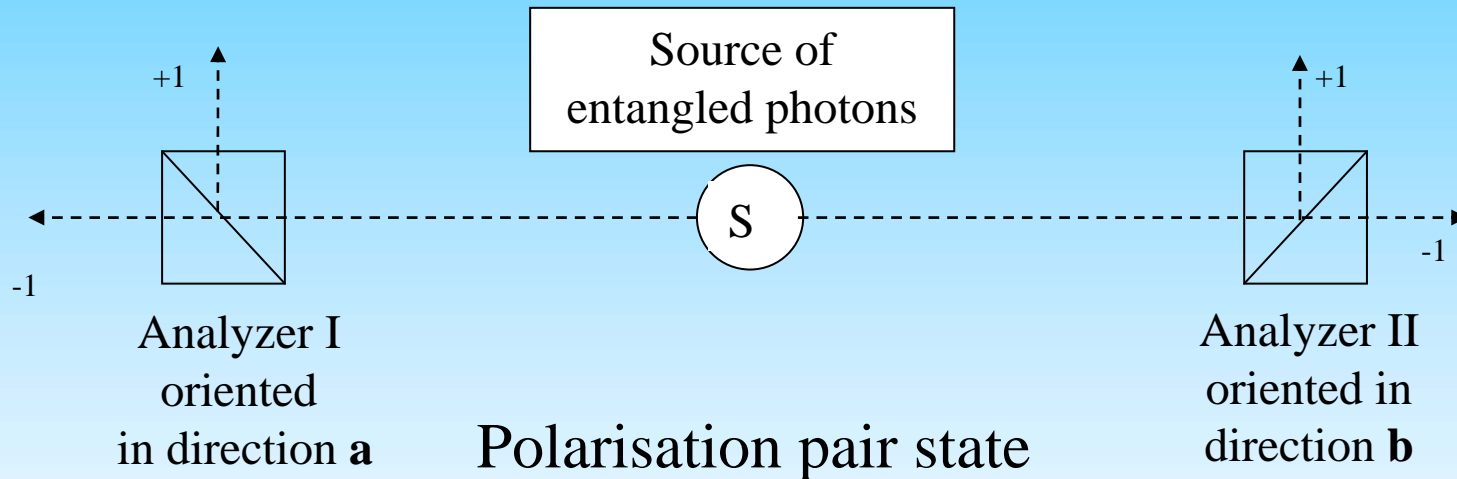
22/10/2005

Bell Inequalities



What is a test of Bell's inequalities?

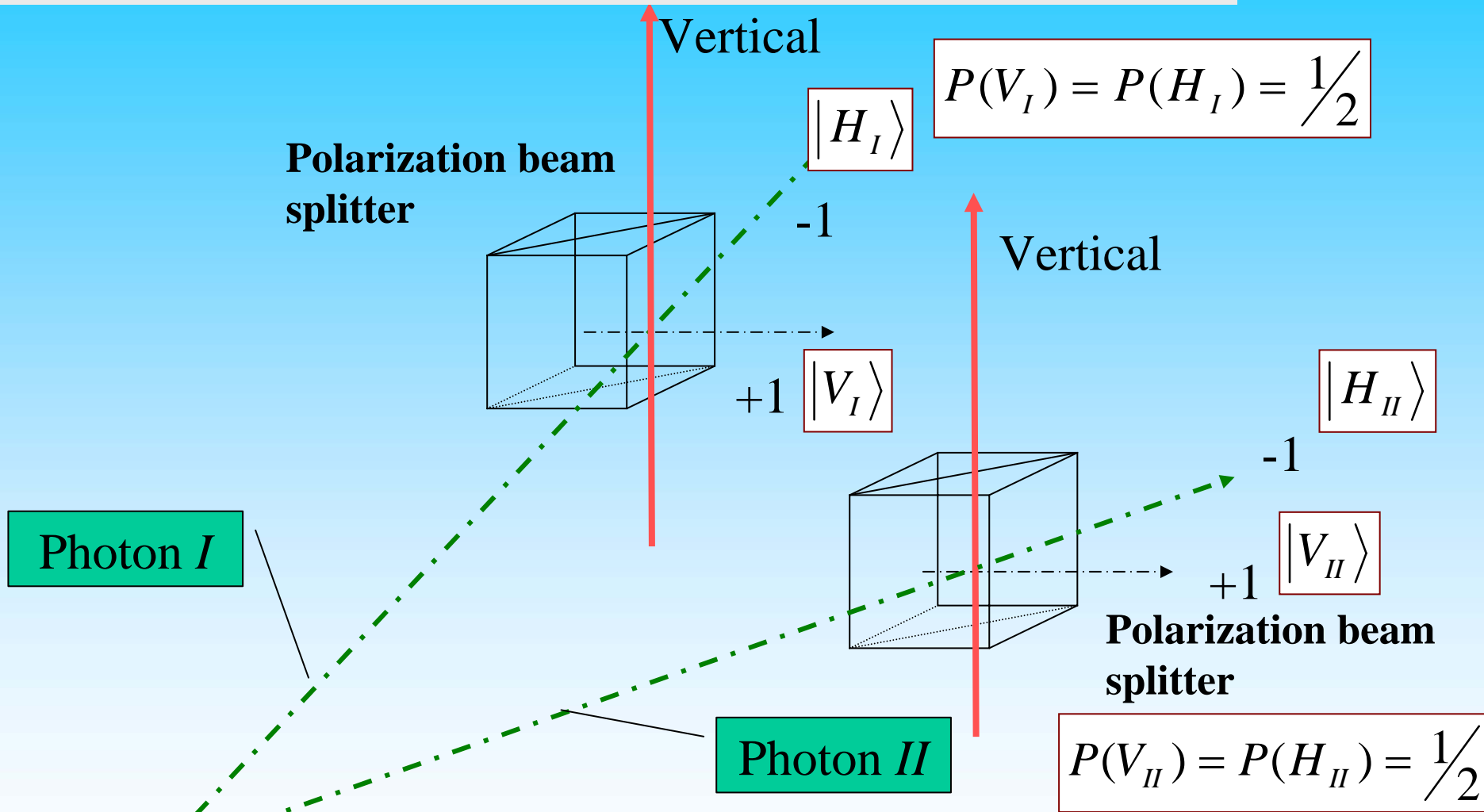
You need a Source of Polarisation-Entangled Photons



$$|\psi\rangle_{EPR} = \frac{1}{\sqrt{2}} (|V_I\rangle|V_{II}\rangle + |H_I\rangle|H_{II}\rangle)$$

Creation of polarization-entangled photons in an EPR state and measurement of joint probabilities of detection for different directions of the 2 analyzers.

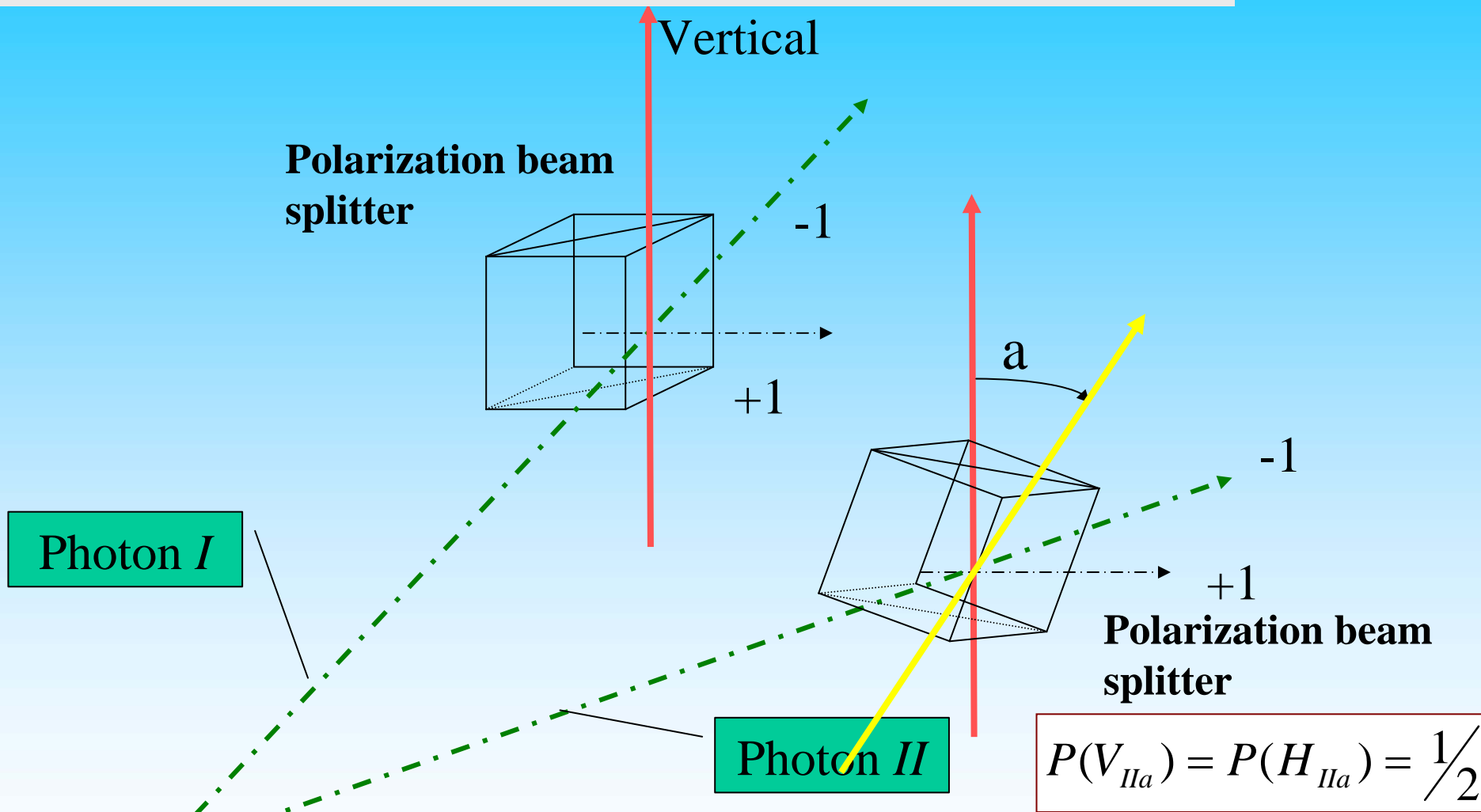
Individual probabilities



The Source of Polarisation-Entangled Photons

$$|\psi\rangle_{EPR} = \frac{1}{\sqrt{2}} (|V_I\rangle|V_{II}\rangle + |H_I\rangle|H_{II}\rangle)$$

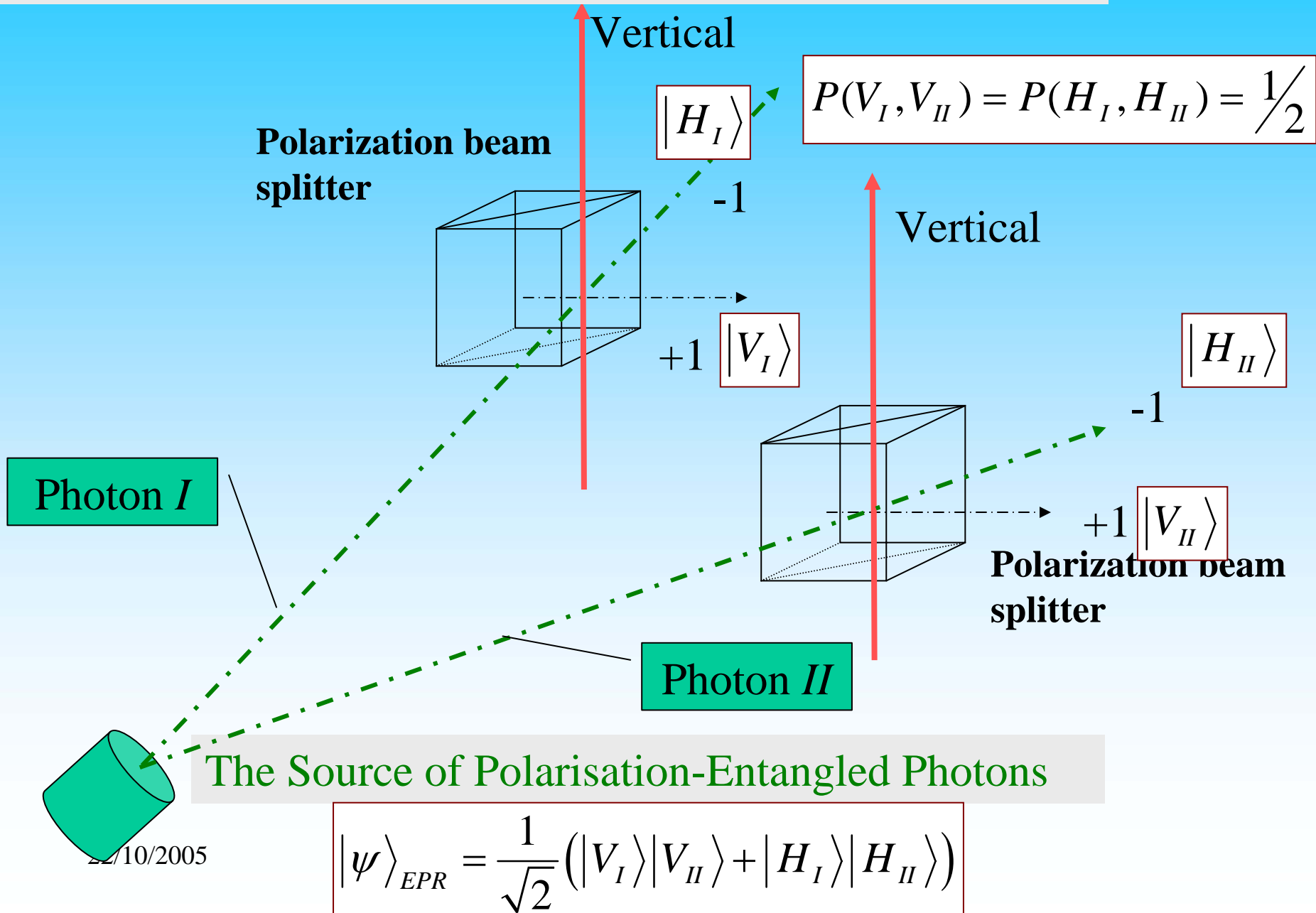
Individual probabilities for any direction a



The Source of Polarisation-Entangled Photons

$$|\psi\rangle_{EPR} = \frac{1}{\sqrt{2}} (|V_I\rangle|V_{II}\rangle + |H_I\rangle|H_{II}\rangle)$$

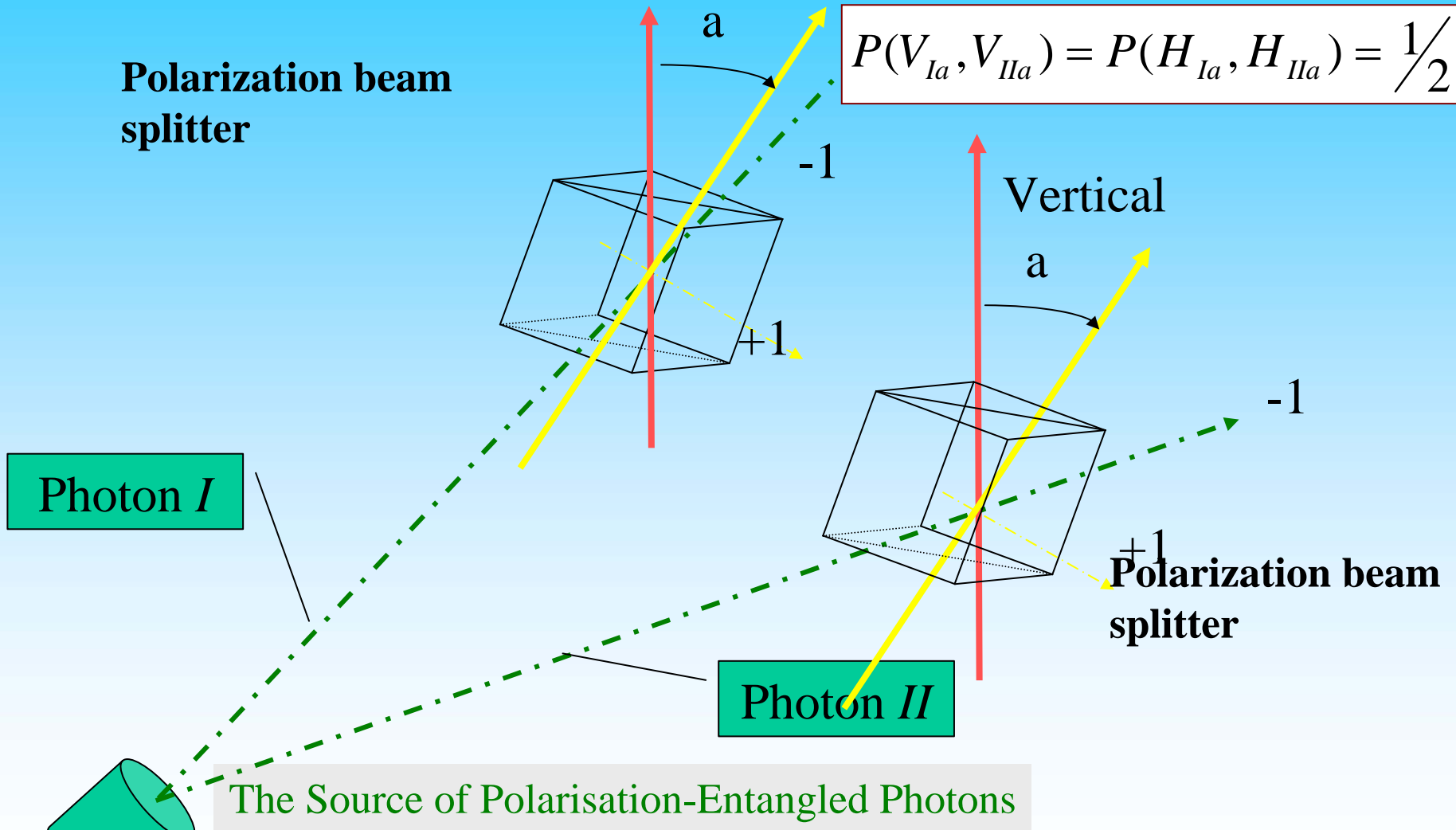
Joint probabilities?



Joint probabilities for any direction a :

$$P(V_{Ia}, V_{IIa}) \text{ or } P(H_{Ia}, H_{IIa}) ?$$

$$P(V_{Ia}, V_{IIa}) = P(H_{Ia}, H_{IIa}) = \frac{1}{2}$$



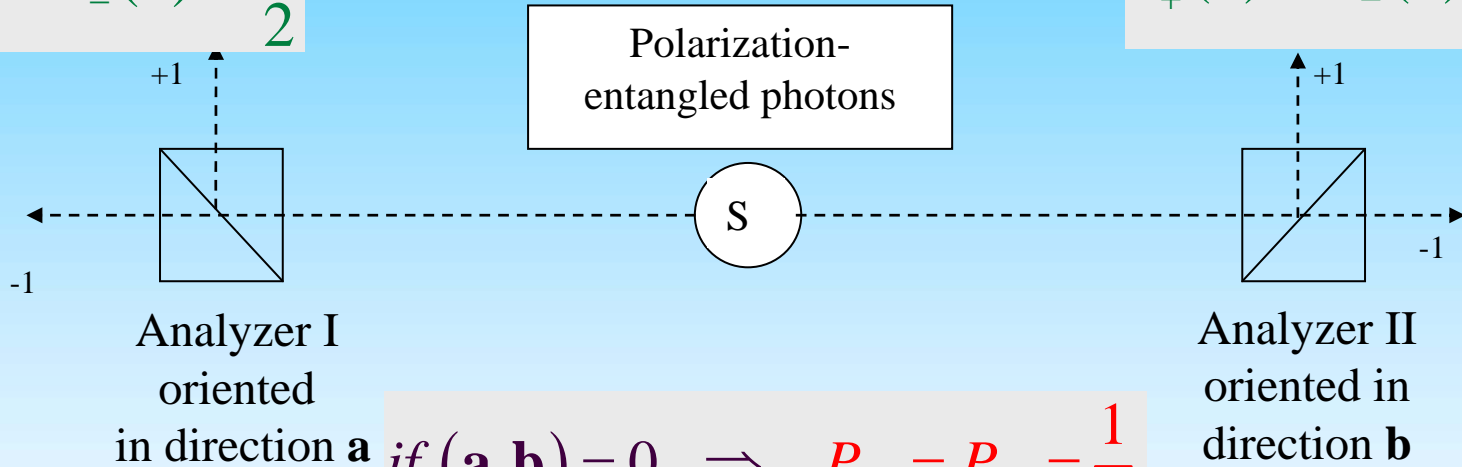
$$|\psi\rangle_{EPR} = \frac{1}{\sqrt{2}} (|V_I\rangle|V_{II}\rangle + |H_I\rangle|H_{II}\rangle)$$

$$|\psi\rangle_{EPR} = \frac{1}{\sqrt{2}} (|V_I\rangle|V_{II}\rangle + |H_I\rangle|H_{II}\rangle)$$

The outstanding properties of this state !

$$P_+(\mathbf{a}) = P_-(\mathbf{a}) = \frac{1}{2}$$

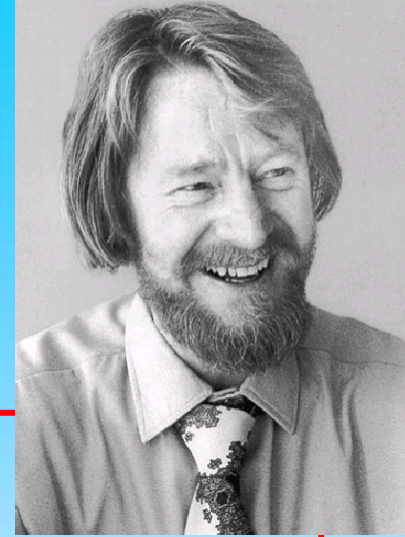
$$P_+(b) = P_-(b) = \frac{1}{2}$$



$$\text{if } (\mathbf{a}, \mathbf{b}) = 0 \Rightarrow \begin{aligned} P_{++} &= P_{--} = \frac{1}{2} \\ P_{+-} &= P_{-+} = 0 \end{aligned}$$

EPR state is characterized by a perfect correlation and a circular symmetry : the joint detection probabilities is always be 0.5 if the analyzers are parallel.

What is a test of Bell's inequalities?



You can measure the degree of correlation :

$$E(a, b) = P(a, b) + P(a_{\perp}, b_{\perp}) - P(a, b_{\perp}) - P(a_{\perp}, b)$$

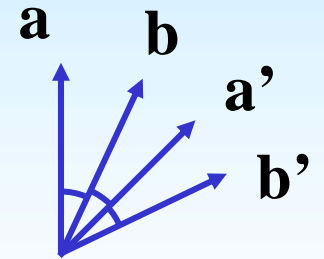
Classical theory :

$$-2 \leq S \leq 2 \quad \text{avec} \quad S = E(\mathbf{a}, \mathbf{b}) - E(\mathbf{a}, \mathbf{b}') + E(\mathbf{a}', \mathbf{b}) + E(\mathbf{a}', \mathbf{b}')$$

Quantum Mechanics $E_{\text{MQ}}(\mathbf{a}, \mathbf{b}) = \cos 2(\mathbf{a}, \mathbf{b})$

For these directions $(\mathbf{a}, \mathbf{b}) = (\mathbf{b}, \mathbf{a}') = (\mathbf{a}', \mathbf{b}) = \frac{\pi}{8}$

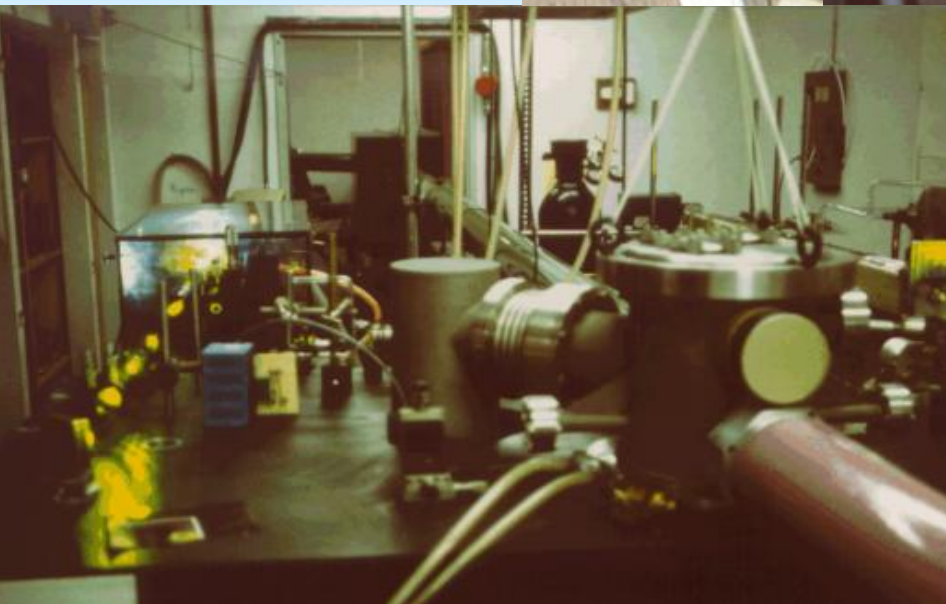
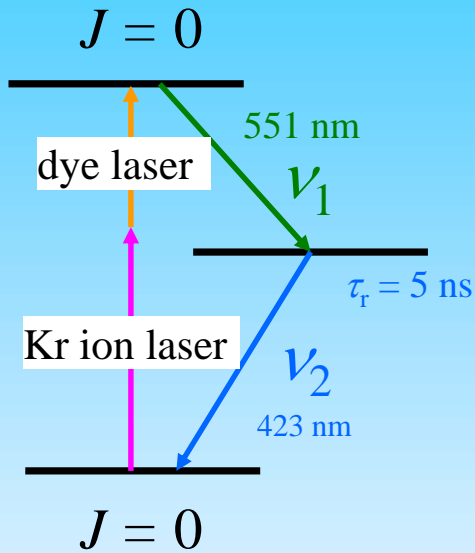
$$S_{\text{QM}} = 2\sqrt{2} = 2.828... > 2$$



Excel Simulation : Alain Vivier

[Expérience Alain Aspect 2](#)

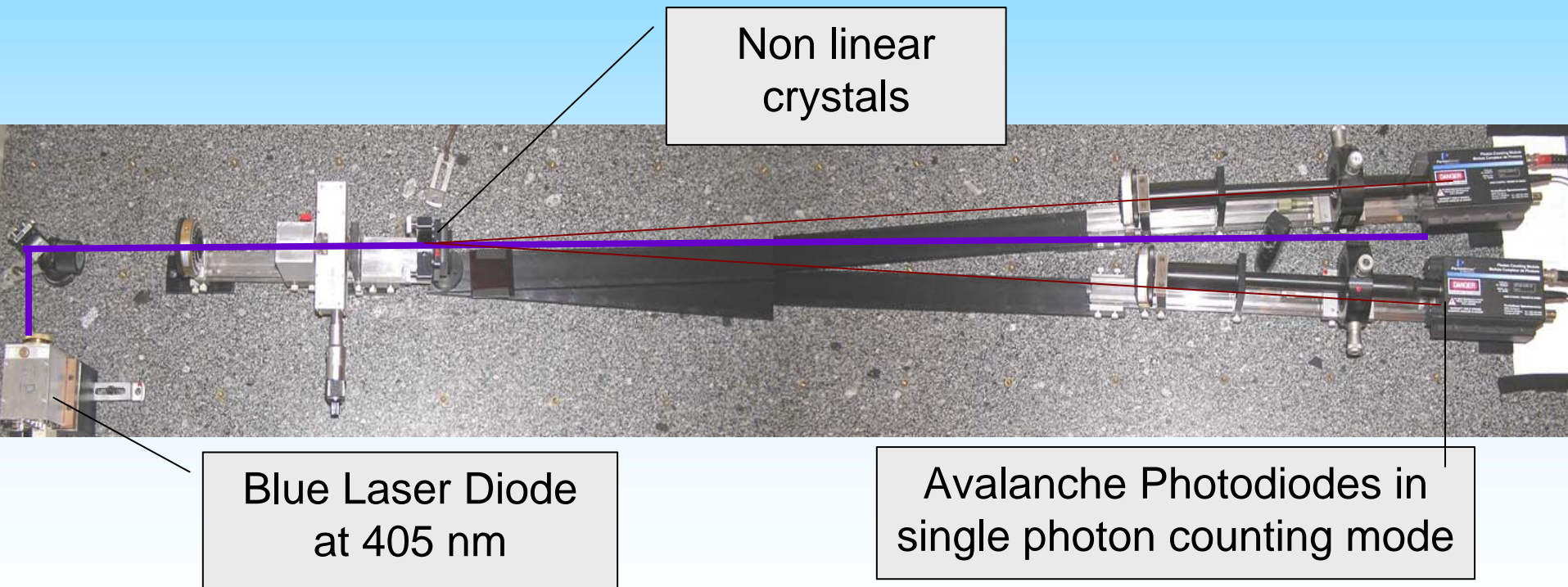
The Orsay source of entangled photons



Alain Aspect, Philippe Grangier in Institut d'Optique

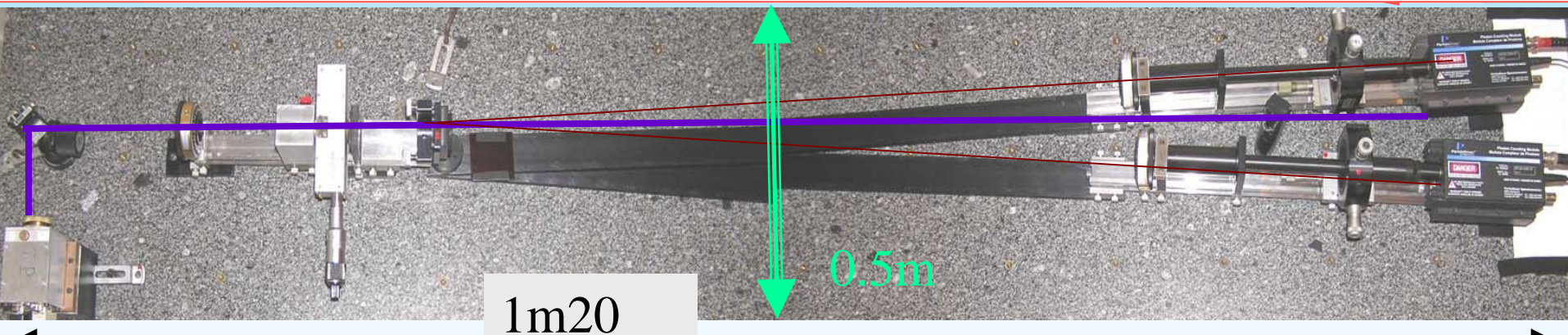
First convincing violations of Bell inequalities

Twenty five years later, due to recent advances in laser diode technology, new techniques for generation of photon pairs and avalanche photodiodes, this experience is now part of the experimental lab course for our students.



Why did we build an entangled photons experiment in our engineering school?

A unique opportunity to deal with **entanglement concept** and **experimental techniques** on polarization, non linear effects, photon counting avalanche photodiodes, counting statistics!



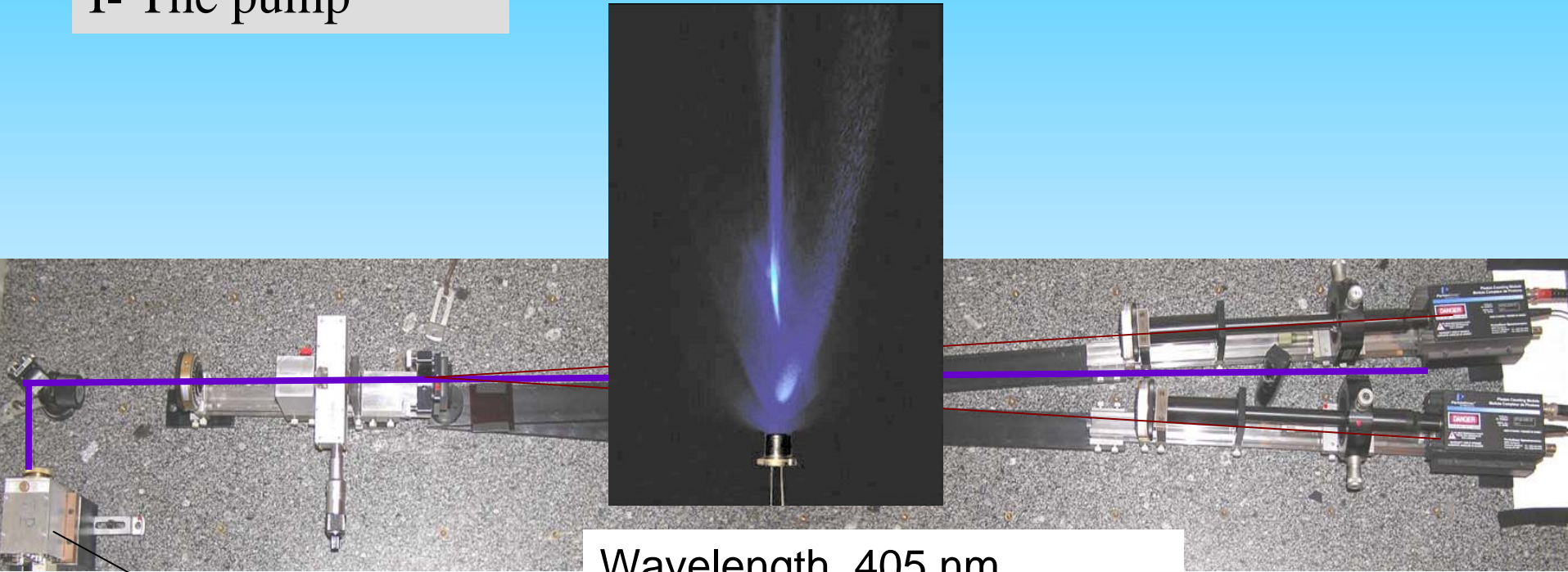
Entangled photons, nonlocality and Bell inequalities in the undergraduate laboratory (Dietrich Dehlinger, M. W. Mitchell)

Physics Department, Portland, Oregon

Quantum Physic (27 May 2002)

The source of polarization-entangled photon pairs

I- The pump



Blue Laser diode
at 405 nm

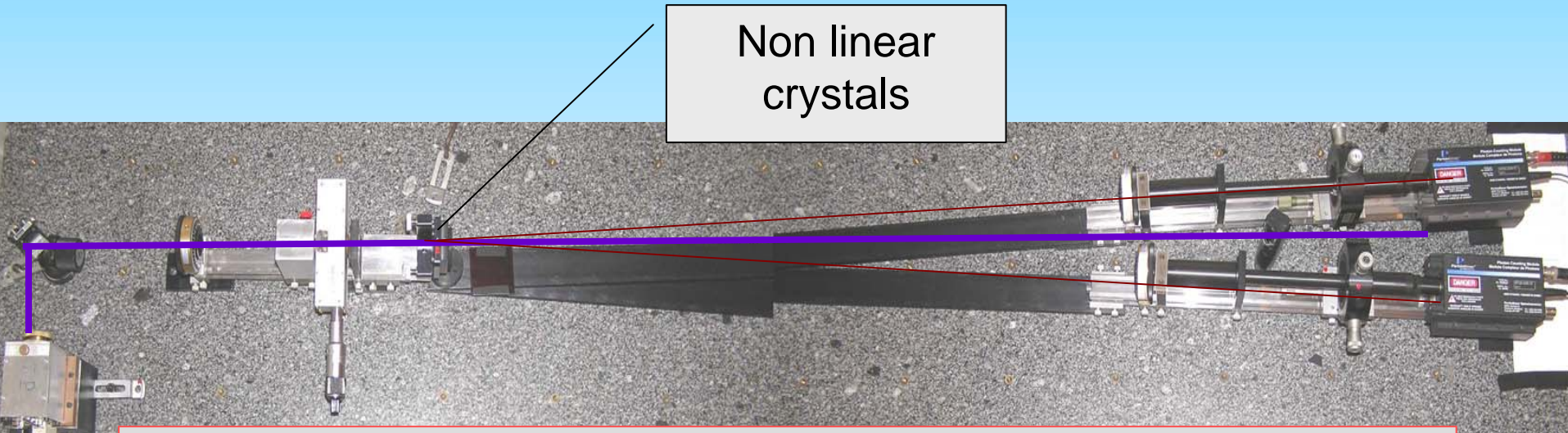
Wavelength 405 nm
Power : 5 mW to 60 mW

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$$N_{\text{pump photons}} = \frac{P}{h\nu} \approx 10^{17} \text{ photons/second}$$

The source of polarization-entangled photon pairs

II- The crystals



Creation of photon pairs : non linear optics

Non linear effect : Spontaneous Parametric Downconversion

Spontaneous Parametric Downconversion in crystals of β -BBO

Type I Phase Matching

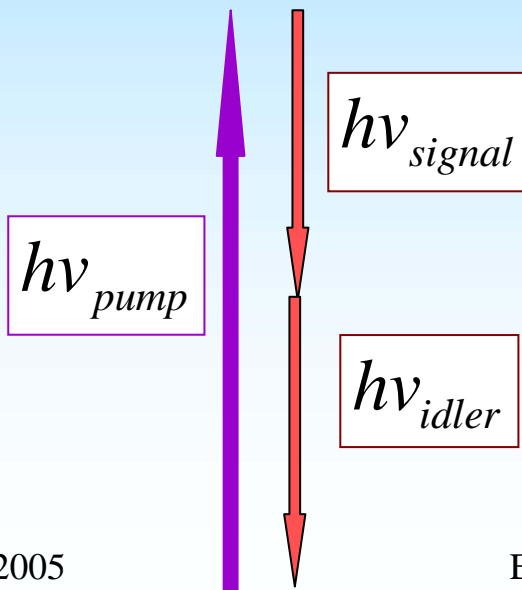
- Energy Conservation :

$$\frac{hc}{\lambda_{pump}} = \frac{hc}{\lambda_{signal}} + \frac{hc}{\lambda_{idler}}$$

$$\lambda_{pump} = 405 \text{ nm}$$

$$\lambda_{signal} = 810 \text{ nm}$$

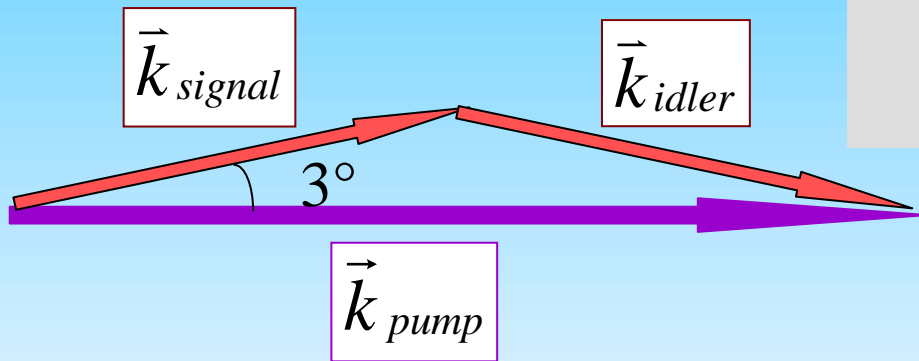
$$\lambda_{idler} = 810 \text{ nm}$$



Degenerate case :
idler and signal have
the same wavelength

- Photon momentum conservation :

$$\frac{2\pi n_e}{\lambda_{pump}} \vec{u}_{idler} = \frac{2\pi n_o}{\lambda_{signal}} \vec{u}_{signal} + \frac{2\pi n_o}{\lambda_{idler}} \vec{u}_{idler}$$



β -BBO is birefringent crystal
negative uniaxe ($n_e < n_o$)

The crystal is cut with the axis at
 30° from pump beam

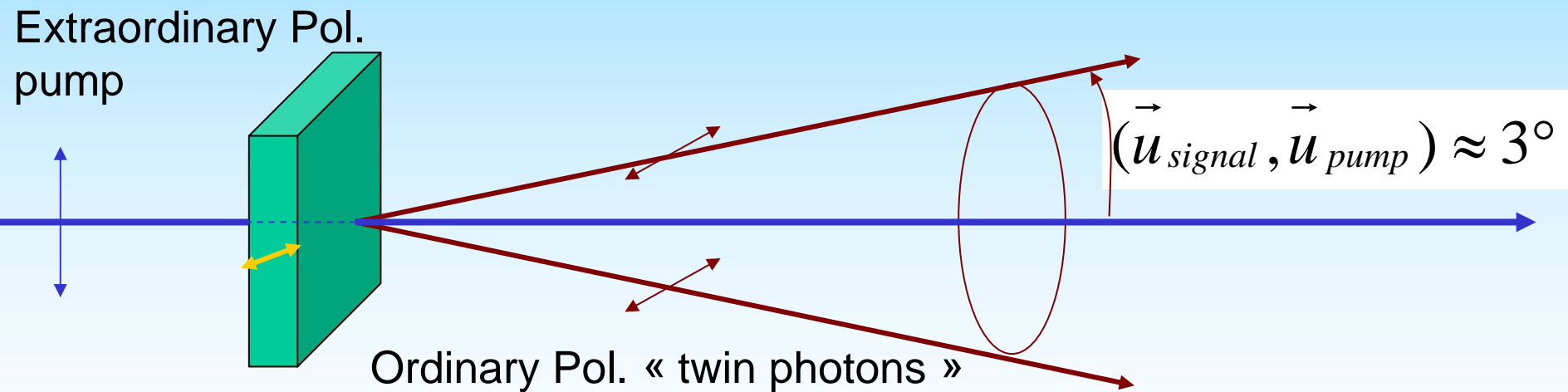
- **Type I phase matching** : « twin » photons are in the same state of polarization.

β -BBO : type I phase matching

β -BBO is birefringent crystal
negative uniaxial ($n_e < n_o$)

$$\frac{n_e}{\lambda_{405nm}} = 2 \frac{n_o}{\lambda_{810nm}} \cos(\vec{u}_{signal}, \vec{u}_{pump})$$

The crystal is cut with the axis at
 30° from pump beam

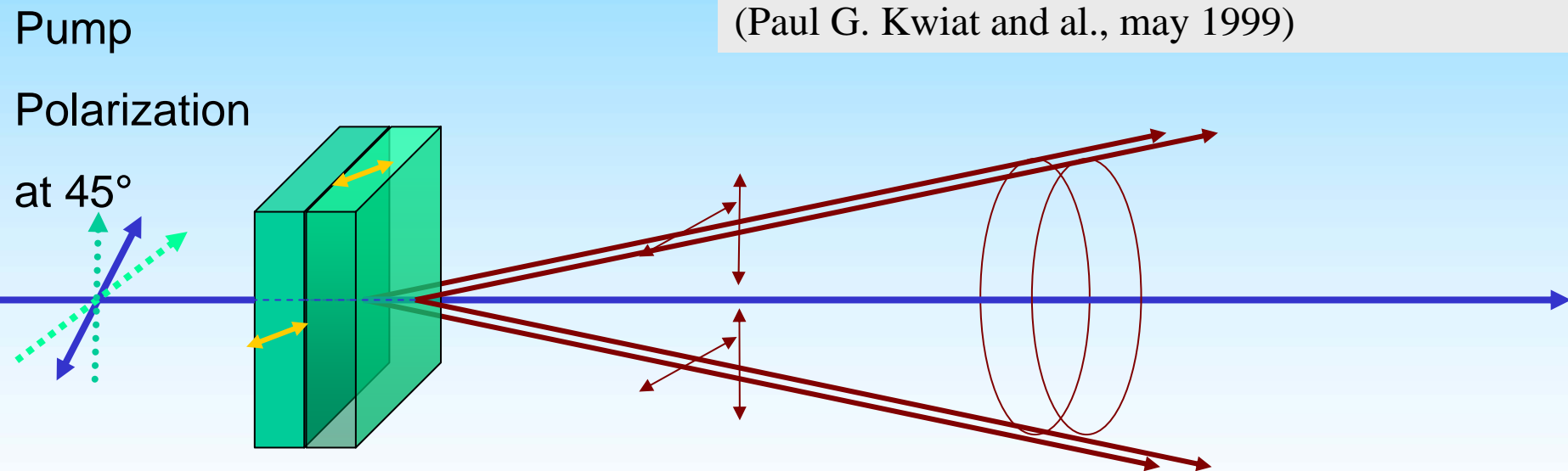


You get same polarization photon pairs

The source of polarization-entangled photon pairs

2 identical BBO crystals : *the second one is rotated by 90°*

Ultra-bright source of polarization-entangled photons
(Paul G. Kwiat and al., may 1999)



With 2 identical BBO crystals
Axis at 30° from pump beam
5 mm x 5 mm and 0,5 mm thick

III- The detectors

Filters at 810 nm and lenses

Polarisation analyzers

Non linear
crystals

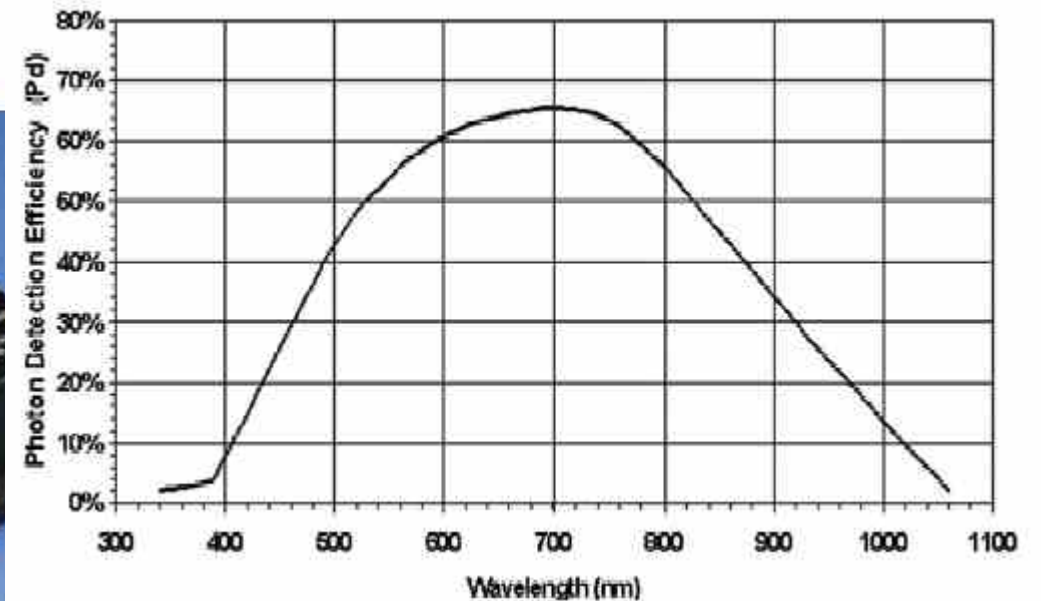
Blue Laser diode
at 405 nm

Single Photon Counting
Module

SPCM avalanche photodiode

Single Photon Counting Module

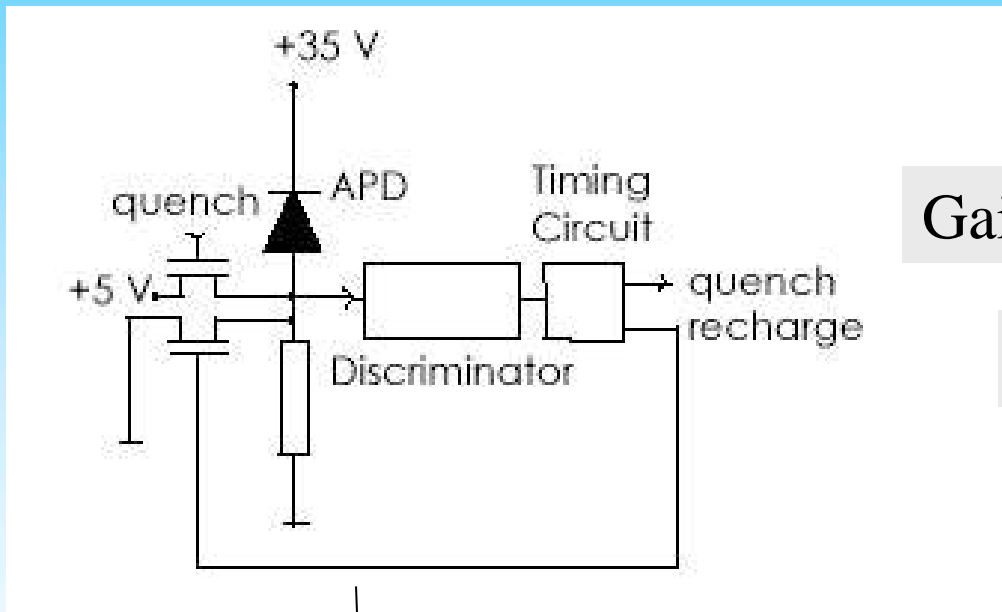
SPCM-AQR Series



Dark counts < 500 cps/s

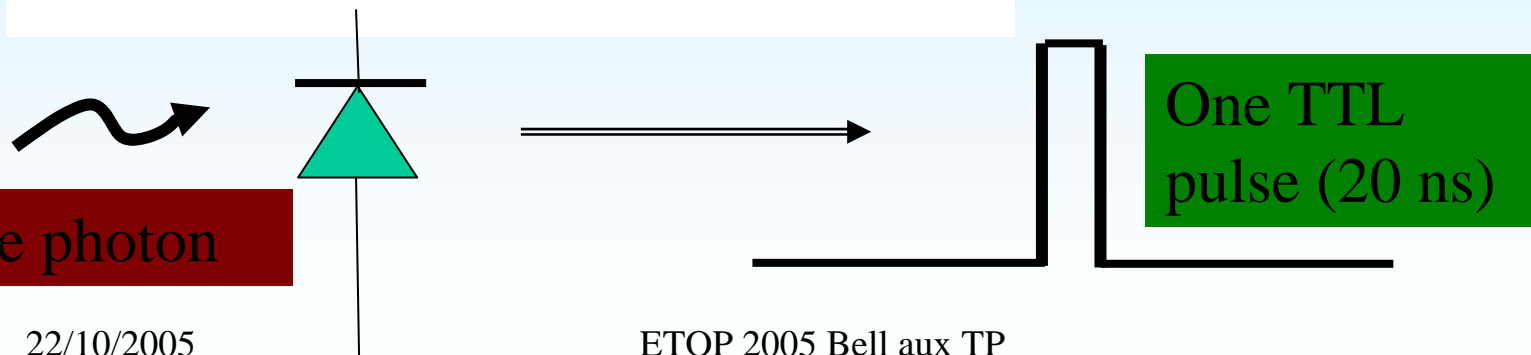
Saturation : $5 \cdot 10^6$ cps/s

Active quenching



Gain : $10^8 - 10^9$

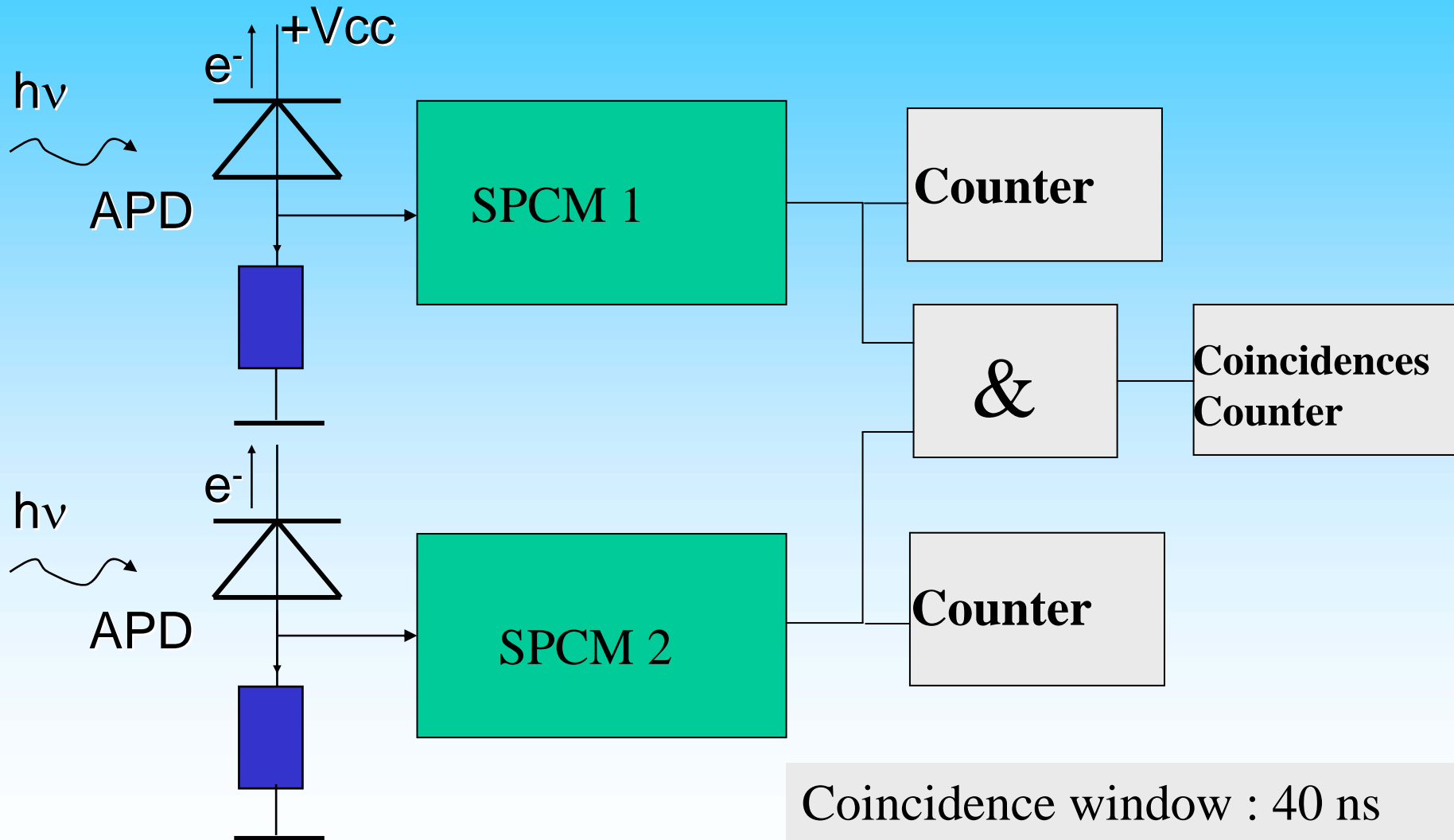
Reset : 75 ns



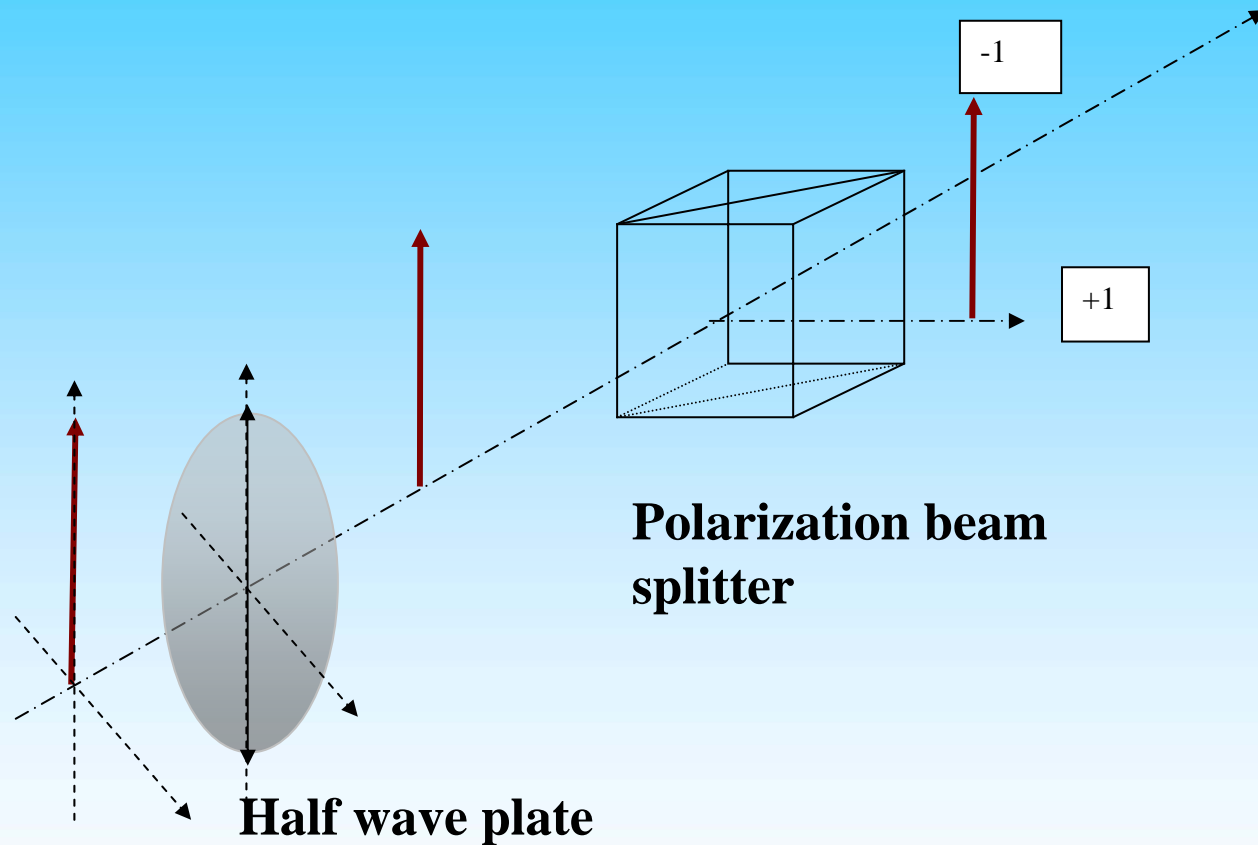
One photon

One TTL pulse (20 ns)

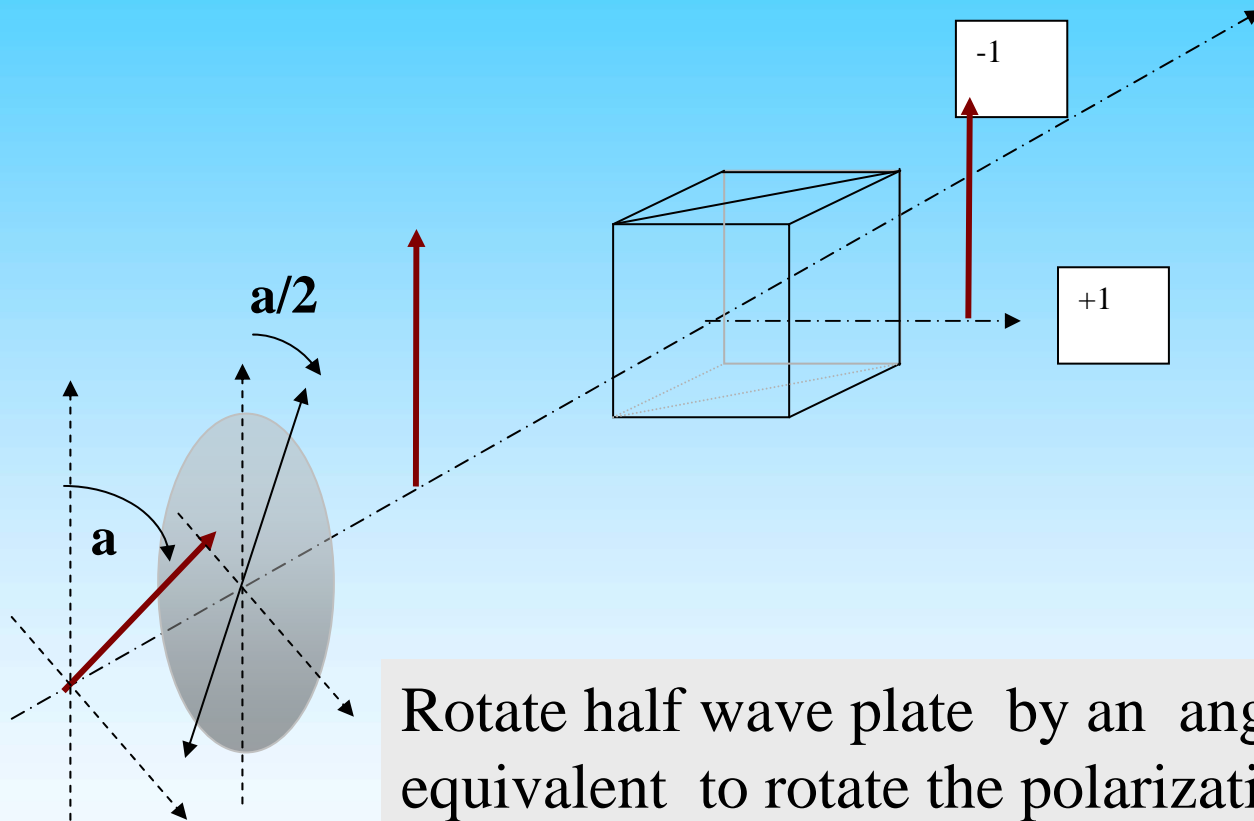
Coincidences Detection



Polarization analyzers



Polarization analyzers

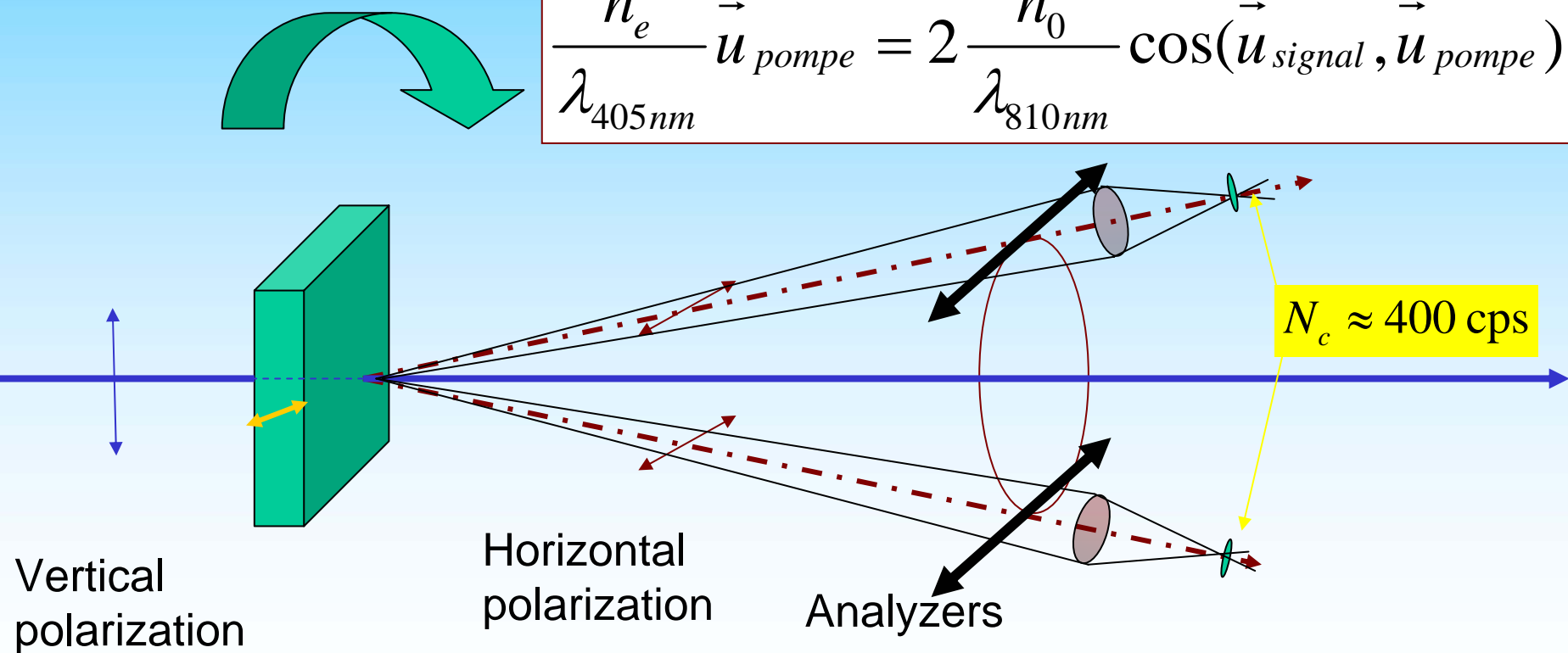


Rotate half wave plate by an angle $a/2$ is equivalent to rotate the polarization beam splitter by an angle a .

IV- Adjustments of the polarization-entangled photon pair source

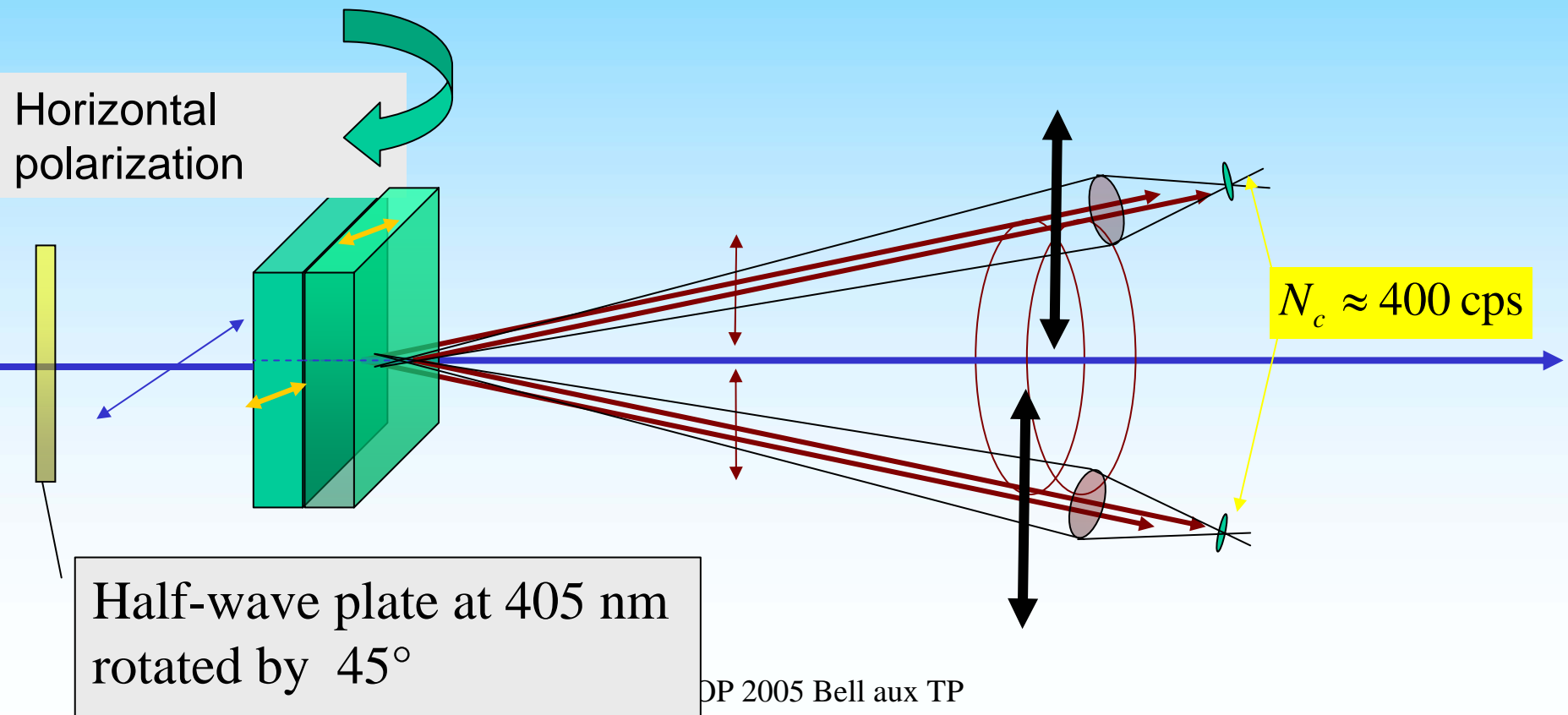
Phase matching in the vertical crystal

$$\frac{n_e}{\lambda_{405nm}} \vec{u}_{pompe} = 2 \frac{n_o}{\lambda_{810nm}} \cos(\vec{u}_{signal}, \vec{u}_{pompe})$$



IV- Adjustments of the polarization-entangled photon pair source

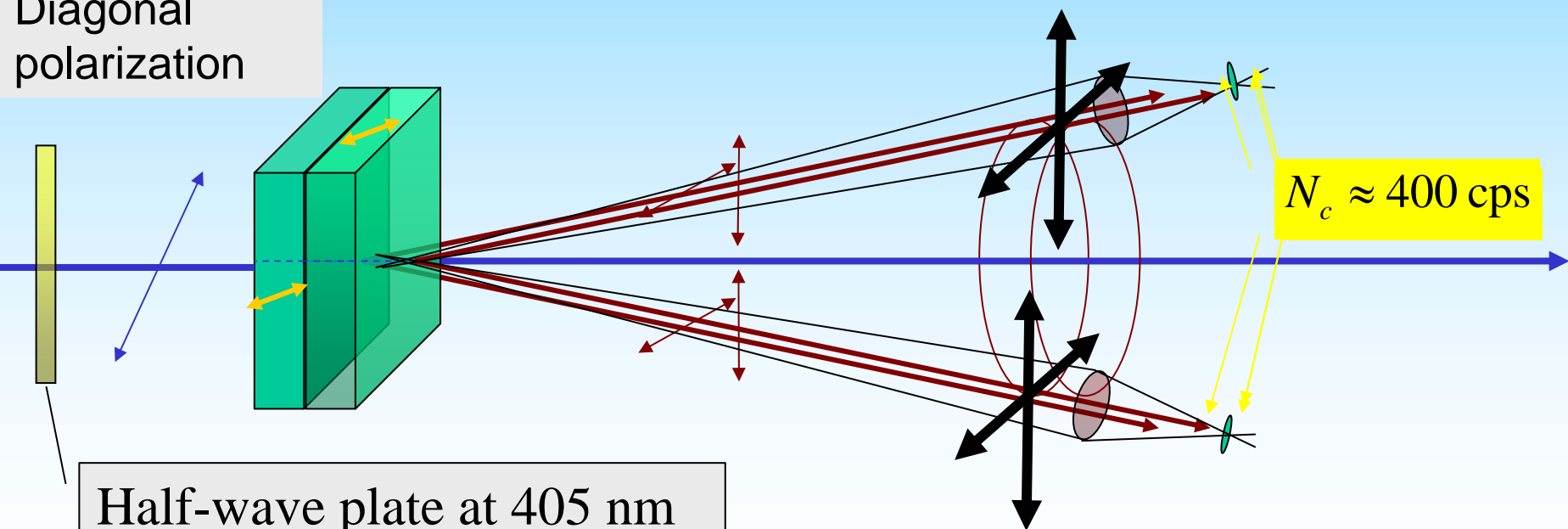
Phase matching in the horizontal crystal



IV- Adjustments of the polarization-entangled photon pair source

We try to count as many vertical pairs as horizontal pairs of entangled photons :
same coincidences rate

Diagonal polarization



Half-wave plate at 405 nm rotated by 22.5° to get a diagonal pump

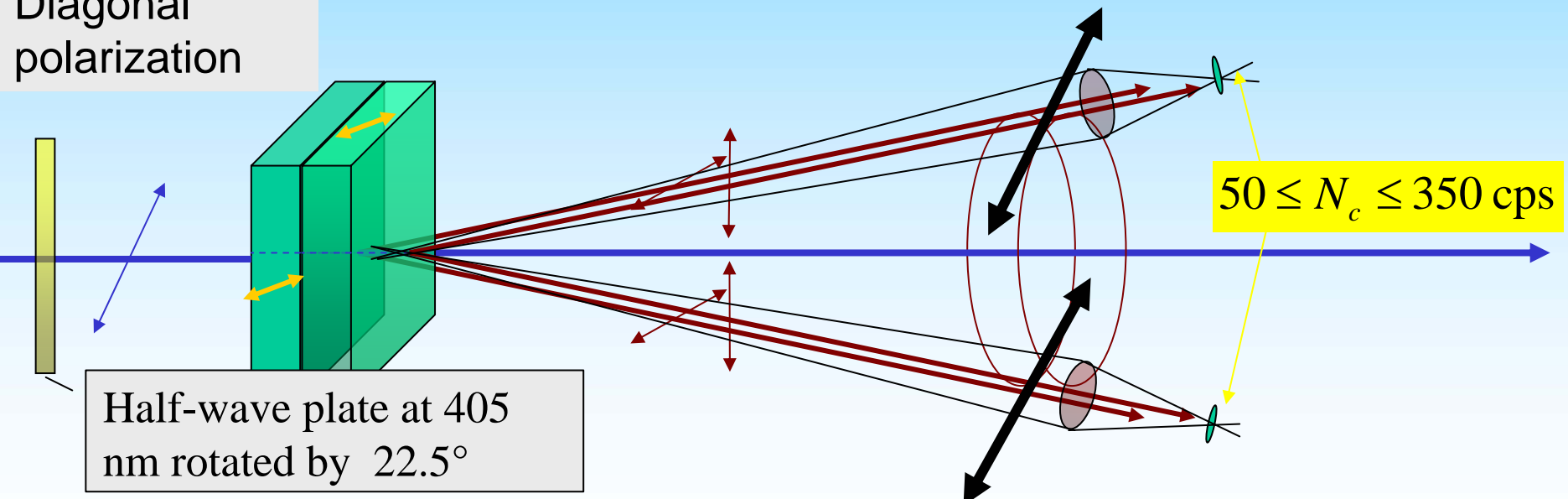
IV- Adjustments of the polarization-entangled photon pair source

But,

when the analyzers are in the diagonal base :

We don't get the same number of photon pairs !

Diagonal polarization



Remember ! EPR state is characterized by a circular symmetry : the joint detections probabilities should always be 0.5 if the analyzers are parallel.

State of the photon pairs !

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|V_I\rangle|V_{II}\rangle + e^{i\phi} |H_I\rangle|H_{II}\rangle)$$



Analyzer 1



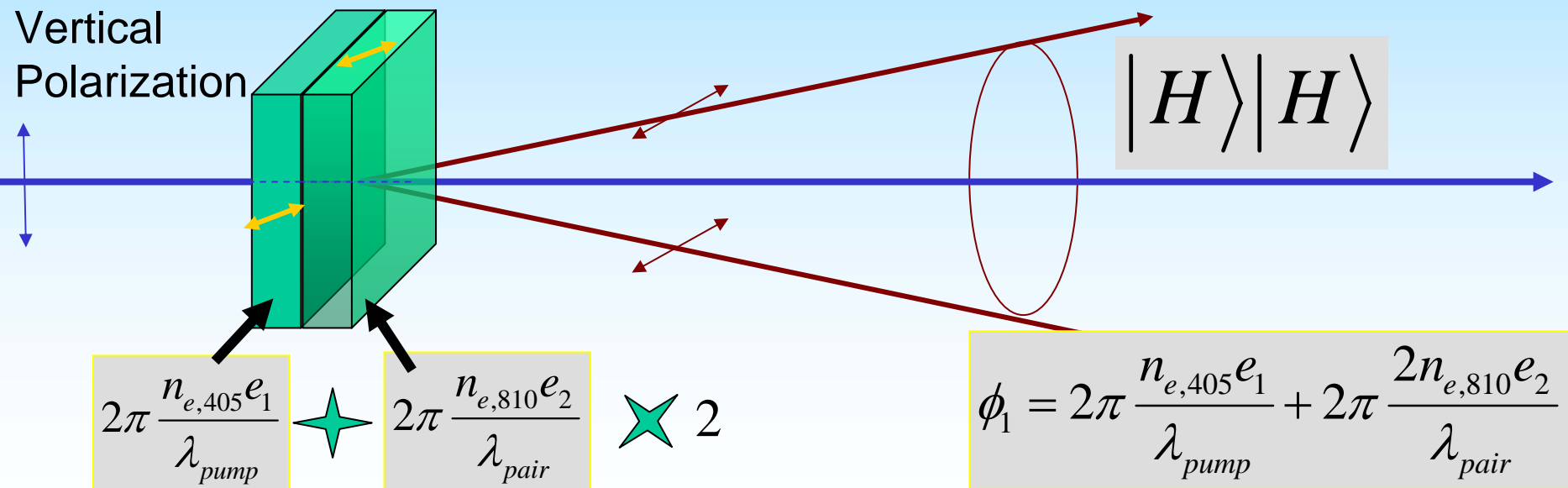
Analyzer 2

Phase between the
2 processes of
pair creation

$$P(V_{I\ 45^\circ}, V_{II\ 45^\circ}) = \frac{1}{4} (1 + \cos \phi)$$

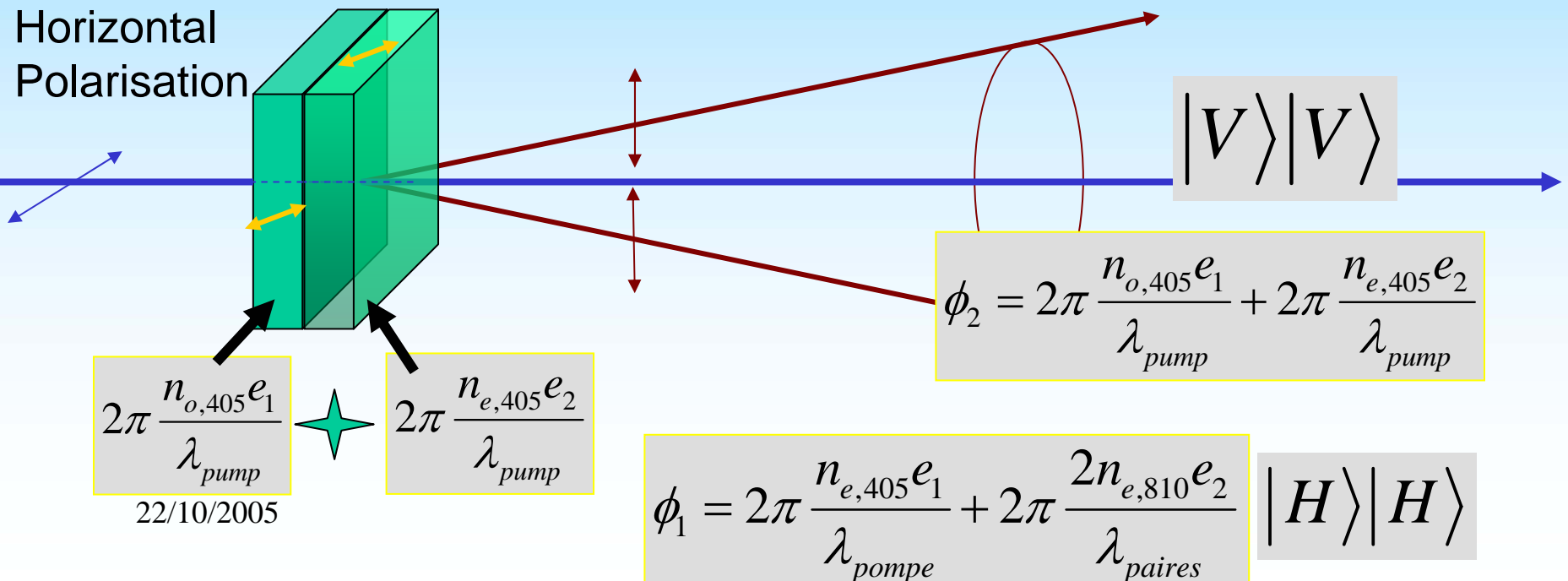
Where does this phase between the 2
processes come from ?

Phase between the 2 processes



Phase between the 2 processes

$$\left\{ \begin{array}{l} \text{Creation process in the vertical crystal : } |V\rangle_{pompe} \rightarrow e^{i\phi_1} |H_I\rangle|H_{II}\rangle \\ \text{Creation process in the horizontal crystal : } |H\rangle_{pompe} \rightarrow e^{i\phi_2} |V_I\rangle|V_{II}\rangle \end{array} \right.$$



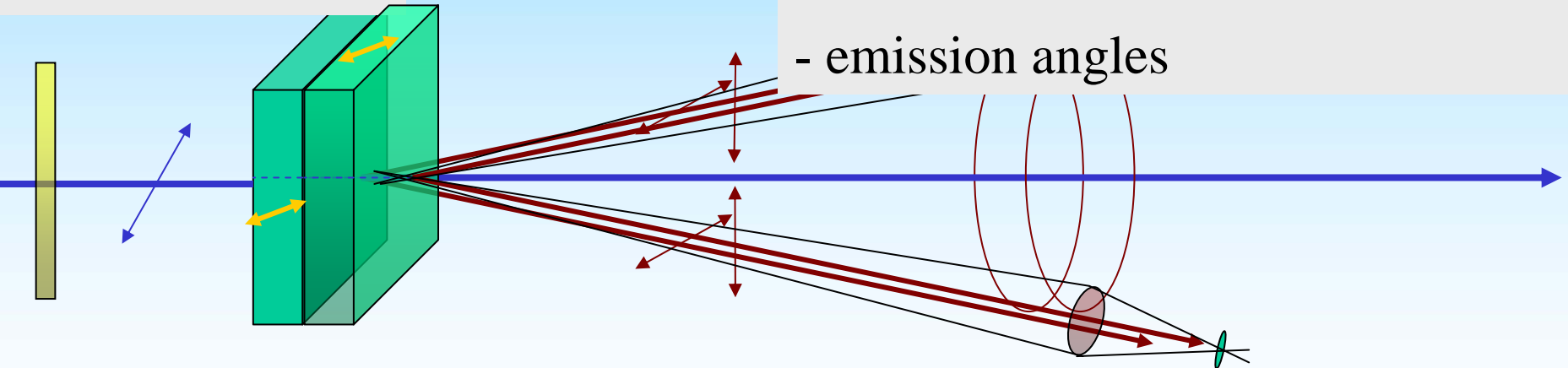
Phase between the 2 processes

$$\phi = \phi_2 - \phi_1 = 2\pi \frac{n_{o,405}e_1}{\lambda_{pump}} + 2\pi \frac{n_{e,405}e_2}{\lambda_{pump}} - 2\pi \frac{n_{e,405}e_1}{\lambda_{pump}} - 2\pi \frac{2n_{e,810}e_2}{\lambda_{pair}}$$

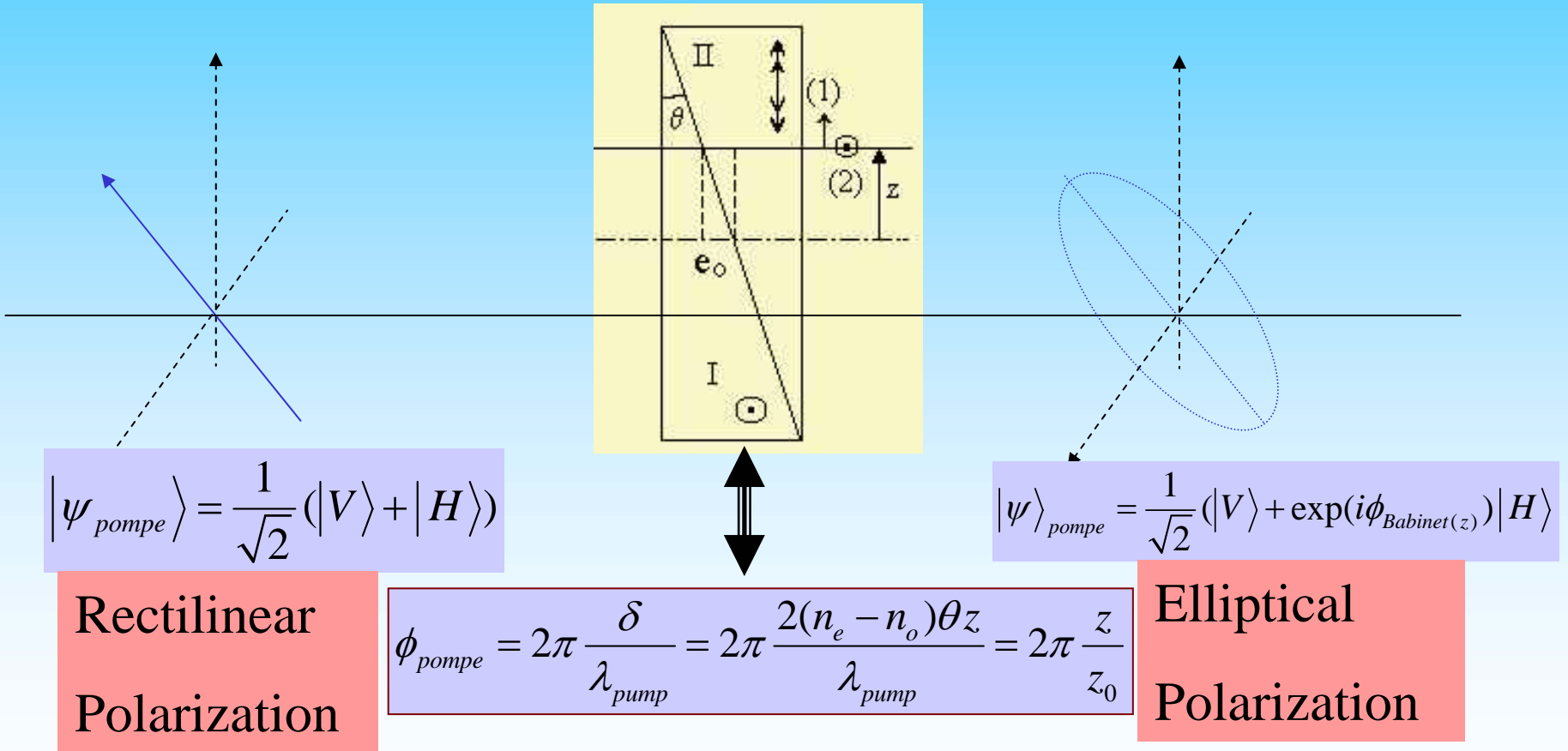


- Depends on :
- pump wavelength
 - photon pairs wavelength
 - crystal thicknesses
 - emission angles

Diagonal
Polarization



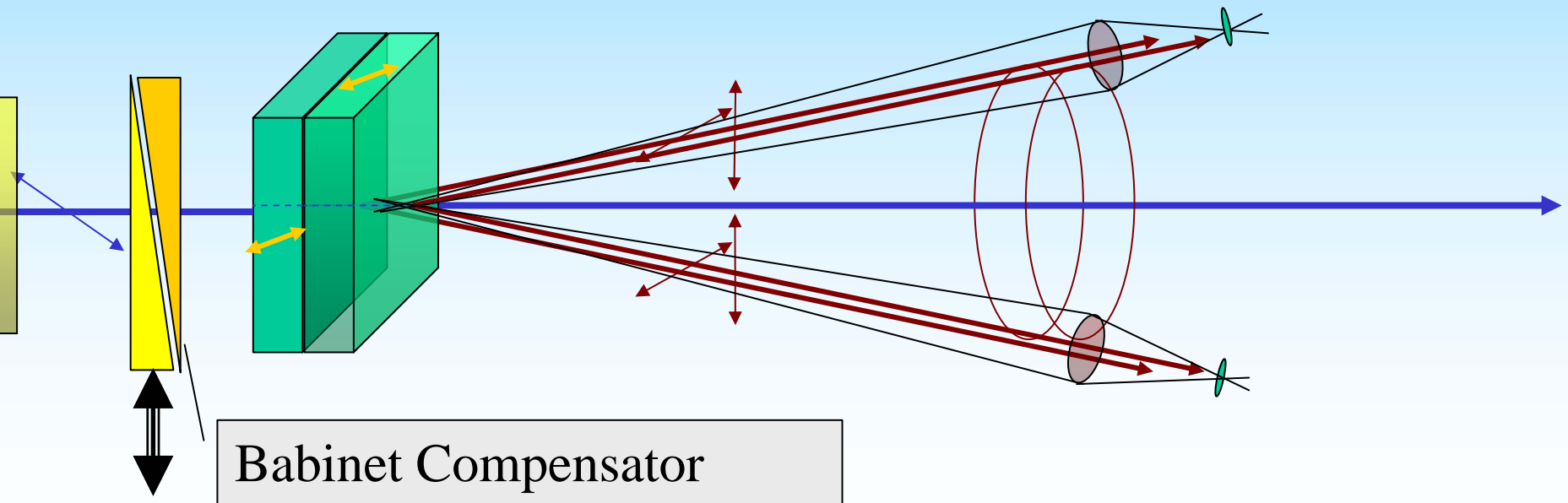
Babinet Compensator



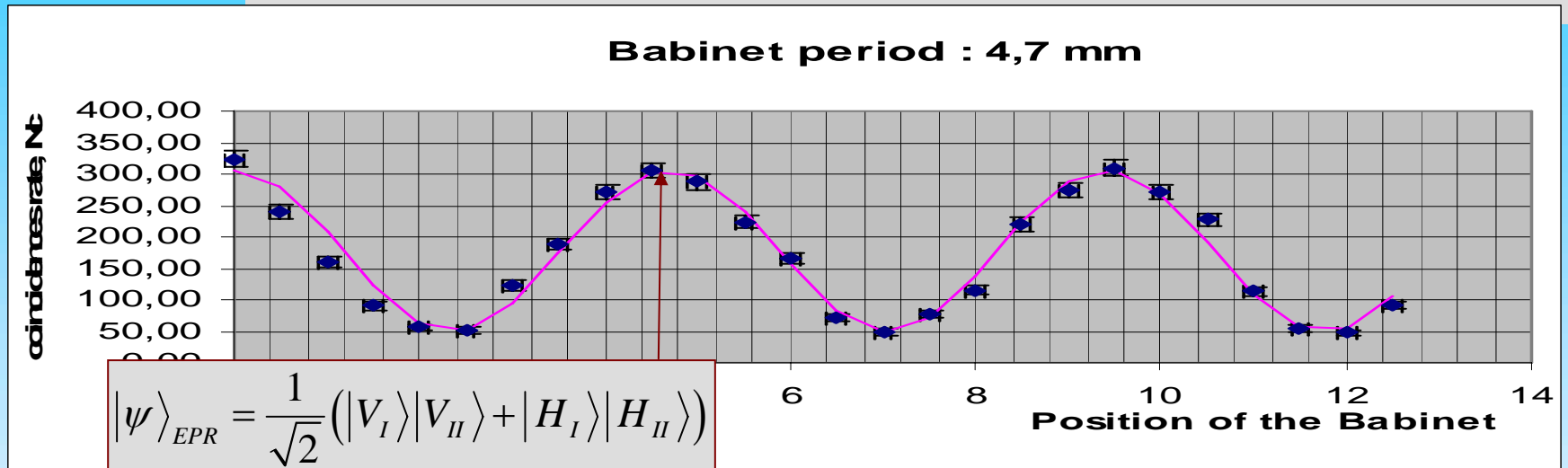
Adjustment of this phase by a Babinet compensator on pump beam

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|V_I\rangle|V_{II}\rangle + e^{i(\phi + \phi_{Babinet}(z))} |H_I\rangle|H_{II}\rangle)$$

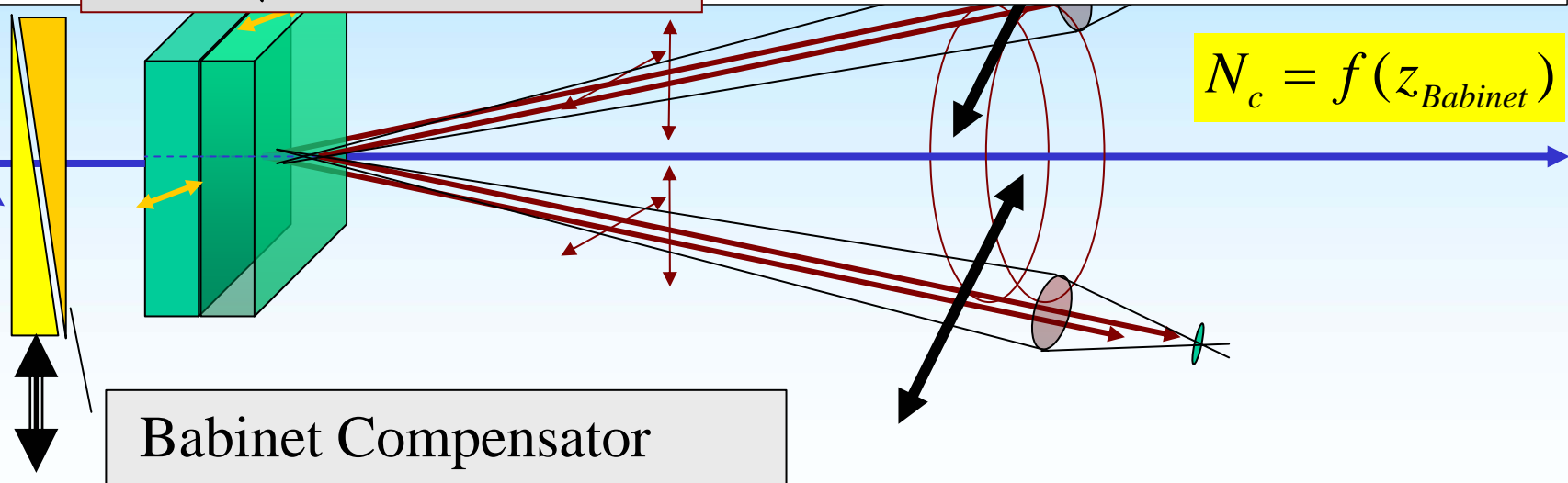
$$|\psi\rangle = |\psi_{EPR}\rangle \text{ if } \phi + \phi_{Babinet} = 2k\pi$$



Adjustment of this phase by a Babinet compensator on pump beam



$$N_c = f(z_{Babinet})$$



V- A test of Bell inequalities

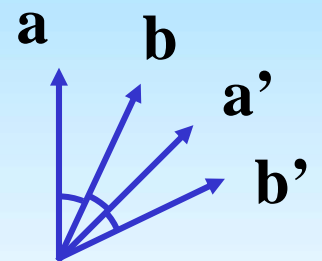
Bell inequalities :

$$-2 \leq S \leq 2 \quad \text{avec} \quad S = E(\mathbf{a}, \mathbf{b}) - E(\mathbf{a}, \mathbf{b}') + E(\mathbf{a}', \mathbf{b}) + E(\mathbf{a}', \mathbf{b}')$$

Quantum Mechanics $E_{\text{MQ}}(\mathbf{a}, \mathbf{b}) = \cos 2(\mathbf{a}, \mathbf{b})$

For the directions $(\mathbf{a}, \mathbf{b}) = (\mathbf{b}, \mathbf{a}') = (\mathbf{a}', \mathbf{b}) = \frac{\pi}{8}$

$$S_{\text{QM}} = 2\sqrt{2} = 2.828... > 2$$



$$E(a, b) = P(a, b) + P(a_{\perp}, b_{\perp}) - P(a, b_{\perp}) - P(a_{\perp}, b)$$

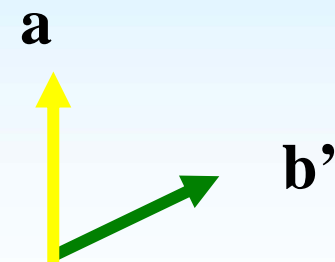
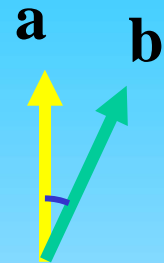
$$E(a, b) = \frac{N(a, b) + N(a + 90, b + 90) - N(a, b + 90) - N(a + 90, b)}{N(a, b) + N(a + 90, b + 90) + N(a, b + 90) + N(a + 90, b)}$$

We need 16 coincidences rate measurements to determine S.

An example of measurements

$$S = E(\mathbf{a}, \mathbf{b}) - E(\mathbf{a}, \mathbf{b}') + E(\mathbf{a}', \mathbf{b}) + E(\mathbf{a}', \mathbf{b}')$$

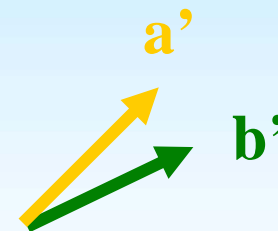
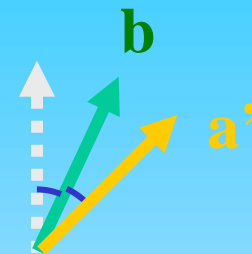
| T (s) | | 10 | | |
|-------------|----------------|-----|-----------|---------------|
| | | nc | sigma(nc) | P(a,b) |
| aV = 0° | bV = 22,5° | 258 | 5,08 | 0,390 |
| aH = 0°+90° | bH = 22,5°+90° | 299 | 5,47 | 0,452 |
| aH = 0°+90° | bV = 22,5° | 52 | 2,28 | 0,079 |
| aV = 0° | bH = 22,5°+90° | 52 | 2,28 | 0,079 |
| | | 661 | | 0,685 |
| | | nt | | E(a,b) |
| | | nc | sigma(nc) | P(a,b') |
| aV = 0° | bV'=67,5° | 61 | 2,47 | 0,083 |
| aH = 0°+90° | bH'=67,5°+90° | 57 | 2,39 | 0,078 |
| aH = 0°+90° | bV'=67,5° | 293 | 5,41 | 0,401 |
| aV = 0° | bH'=67,5°+90° | 320 | 5,66 | 0,438 |
| | | 731 | | -0,677 |
| | | nt | | E(a,b') |



$$S = E(\mathbf{a}, \mathbf{b}) - E(\mathbf{a}, \mathbf{b}') + E(\mathbf{a}', \mathbf{b}) + E(\mathbf{a}', \mathbf{b}')$$

| | | nc | sigma(nc) | P(a',b) |
|-------------|---------------|-----|-----------|--------------|
| aV'=45° | bV =22,5° | 282 | 5,31 | 0,392 |
| aH'=45°+90° | bH =22,5°+90° | 270 | 5,20 | 0,376 |
| aH'=45°+90° | bV =22,5° | 83 | 2,88 | 0,115 |
| aV'=45° | bH =22,5°+90° | 84 | 2,90 | 0,117 |
| | | 719 | | 0,535 |
| | | nt | | E(a',b) |

| | | nc | sigma(nc) | P(a',b') |
|-------------|---------------|-----|-----------|--------------|
| aV'=45° | bV'=67,5° | 292 | 5,40 | 0,401 |
| aH'=45°+90° | bH'=67,5°+90° | 280 | 5,29 | 0,384 |
| aH'=45°+90° | bV'=67,5° | 78 | 2,79 | 0,107 |
| aV'=45° | bH'=67,5°+90° | 79 | 2,81 | 0,108 |
| | | 729 | | 0,569 |
| | | nt | | E(a',b') |



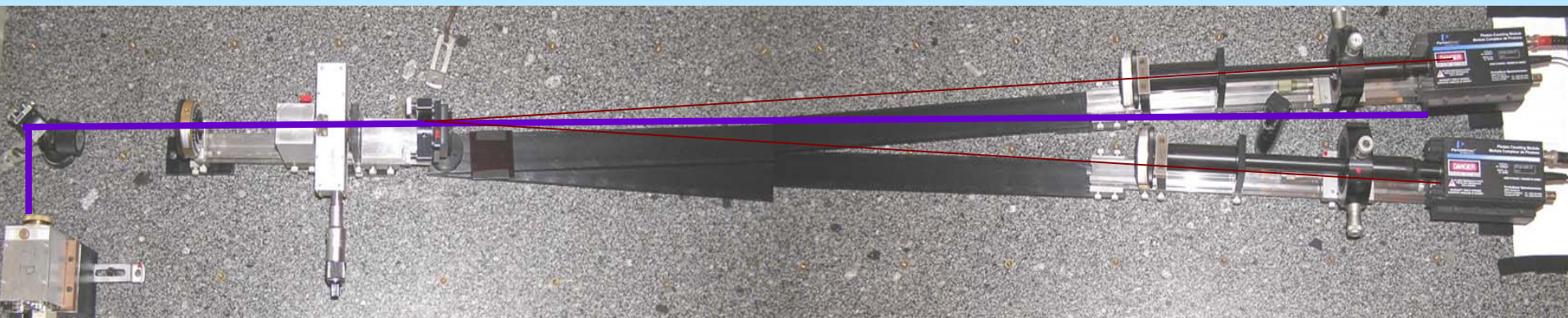
S **2,467**

SM.Q. **2,828**



Bohr - Einstein

From gedankenexperiment (1935)



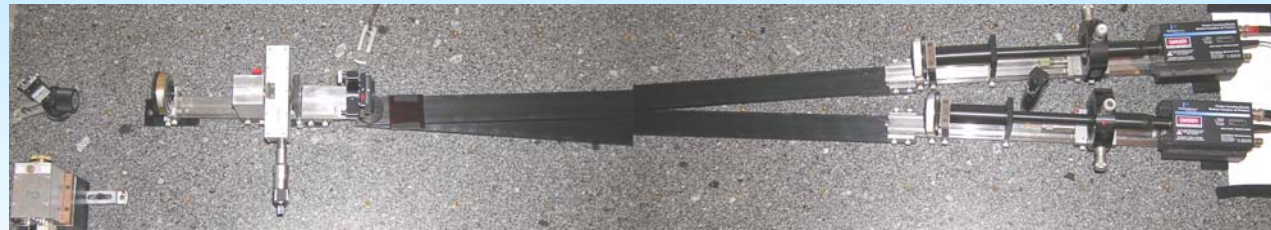
Now a Lab work for students

and a Violation of Bell Inequalities twice a week by them !

http://www.institutoptique.fr/affiche.jsp?folder=ecole_moyens_pedagogiques

Thanks to :

- Alain Aspect
- Philippe Grangier
- André Ducasse
- Thierry Avignon
- Gaetan Messin
-



Students :

Philippe Fereira

Laetitia Mabile